## DEM-CFD Study of Flow in a Random

 Packed Bed Martin Šourek ${ }^{1}$, Martin Isoz ${ }^{1,2}$ ${ }^{1}$ Department of Mathematics, Faculty of Chemical Engineering, University of Chemistry and Technology, Studentska 5, 166 28 Prague, Czech Republic ${ }^{2}$ Institute of Thermomechanics of the Czech Academy of Sciences, Dolejskova 5, 18200 Prague, Czech Republic
## Introduction

Most catalytic surface reactions as well as other industrial applications take advantage of fixed packed bed reactors [6, 3]. Designers of these reactors rely mostly on empirical formulas derived for various simplifying assumptions, e.g. uniformly distributed porosity [2]. The made simplifications and especially the assumption of uniformly distributed porosity fail if the tube to particle diameter ratio goes under 10 and the „wall effect " [1] becomes more significant. In such a case, the complete three-dimensional structure of the packed bed has to be considered.
Thanks to ongoing improvements in numerical mathematics and computational power, the methods of computational fluid dynamics (CFD) have become a great tool for comprehensive description of the packed beds with low tube to particle diameter ratio. Three-dimensional simulations of the flow through two fixed beds differing in the type of the used particle are presented and compared with available experimental and empirical results. To generate the random fixed beds, we propose a custom approach based on the discrete element method (DEM) code implemented in open-source software Blender, see Fig. 1. Thereafter, OpenFOAM tools (snappyHexMesh, simpleFoam) are used for creation of the computational mesh and solution of the governing equations describing a single-phase flow in the packed bed


Figure 1: llustration of studied packings consisting of different type of the used particle. Colors re used to point out different boundaries

## Packed bed geometry generation algorithm (Raschig rings)

Require: Number of vertices in one cylinder numOfVertices $=64$ and number of Raschig rings in geometry numOfRings $=50$
1: Create cylinder with diameter $d_{t}=0.06 \mathrm{~m}$, height $h_{t}=0.1 \mathrm{~m}$ and number of vertices numOfVertices
2: for $i=1$ to $\frac{\text { numOfVertices }}{2}$ do
3: vertices $[i]$.select $\stackrel{2}{=}$ True
4: end for
5: mesh.delete(type='FACE') \{remove top face selected by vertices to create column\}
6: for $i=1$ to numOfRings do
7: Create cylinder with diameter $d_{t}=0.015 \mathrm{~m}$, height $h_{t}=0.015 \mathrm{~m}$ and number of vertices numOfVertices
8: $\quad$ location $=(-0.015+(\operatorname{random}() * 0.03),-0.015+(\operatorname{random}() * 0.03), 0.05+i * 0.017)$ \{relocate cylinder
9: $\quad \operatorname{rotate}(10$, axis $=(\operatorname{random}() * 10, \operatorname{random}() * 10, \operatorname{random}() * 10)\{$ rotate $\}$
10: for $n=1$ to $\frac{\text { num } O f \text { Vertices }}{2}$ \{making hole to cylinder to create Raschig ring\} do
11: vertices[n].select=True
end for
mesh.inset(thickness=0.25) \{inset face on the top of cylinder\}
mesh.delete(type='FACE') \{delete inner face $\}$
for $n=\frac{\text { numofvertices }}{2}+1$ to numOfVertices do
16: $\quad$ vertices $[n]$.select $=$ True
end for
18: mesh.inset(thickness=0.25) \{inset face on the bottom of cylinder\}
19: mesh.delete(type='FACE') \{delete inner face\}
20: end for
21: $\{$ Set properties for physics engine\}
22: bullet.physicsType='RIGID BODY'
23: bullet.useCollisionBounds = True
24: bullet.radius $=0.0035$
25: bullet.velocityMax $=10$ \{for better collision detection\}
26: bullet.collisionMargin $=0.002$ \{detection of overlap\}
27: bullet.formFactor $=0.001$ \{low friction \}
28: Start physics engine until velocities are equal to zero for 10 seconds
29: return Geometry representation of the random packed bed consisting of Raschig rings suitable for the snappyHexMesh utility

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Simulation set up
To estimate the pressure loss over the packed bed, we need to solve a set of isothermal, turbulent, steady-state Navier-Stokes equations for an incompressible Newtonian fluid [5],

$$
\begin{aligned}
\nabla \cdot(\overline{\mathbf{U}} \otimes \overline{\mathbf{U}})-\nabla \cdot\left(\overline{\mathbb{T}}+\mathbb{T}^{\prime}\right) & =-\nabla \bar{p} \\
\nabla \cdot \overline{\mathbf{U}} & =0,
\end{aligned}
$$

where $\mathbb{T}^{\prime}$ is the Reynolds stress tensor. In this work we used the $k-\omega$ SST model [4] for the closure of the problem
The flow governing equations together with the equations for the turbulence variables $k$ and $\omega$ were solved via the simpleFoam solver from the OpenFOAM toolbox. The used finite volume (FV) mesh was created using the snappyHexMesh software, which is available in the OpenFOAM installation. The needed representation of a packing geometry in STL format was prepared via SuperPak type packing geometry generation algorithm implemented in the Blender software. The applied boundary conditions are listed in Tab. 1. As initial guess, we prescribed $\mathbf{U}=(0,0,0)^{\mathrm{T}}, p=0, k=0, \omega=0$ in the whole solution domain.

| Boundary | Colour in Fig. 1 | U | $p$ | $k$ | $\omega$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Inlet | yellow | flowRateInletVelocity | zeroGradient | fixedValue | fixedValue |
| Outlet | red | inletOutlet | fixedValue | inletOutlet | inletOutlet |
| Wals \& Bed | blue \& gray | noSlip | zeroGradient zeroGradient zeroGradient |  |  |

Table 1 : Applied boundary conditions. InletOutlet boundary condition is used for simulation stabilization.


Figure 2 : Result and validation for different types of packed bed


Figure 3 : Pressure field and stream lines in the simulated fixed beds
The kinematic pressure distribution is depicted in the clips in the back of the figures. Stream lines in the front of the images in Fig. 3 show possible trajectories of the flow through fixed bed. The highest velocities occur when the fluid is passing around pellet near contact points of two pellets or near contact points of a pellet and the wall.


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